

Lecture 8:  
Regression Discontinuity, 2 of 2

March 4, 2026

## Course Administration

- ① Problem set 3 should be in
- ② Problem set 3 quiz

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- ⑤ Sign up for consultations
  - April 2, 9 and 10
  - in lieu of class lecture 13
  - see link in lecture 13
  - let me know if more spots needed
- ⑥ Please come see me about your replication paper
- ⑦ Any other issues?

## Lecture 8: RD and RDK

### Background on RD and RDK

- ① RD Recap
- ② Fuzzy RD
- ③ Regression Kink
- ④ How-to, Again
- ⑤ RD vs Diff-in-diff

### Manoli and Turner

- ① Research question, endogeneity and data
- ② Discontinuity, estimating equations, validity
- ③ Results

# RD Recap

What do you need for a RD design?

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- You need a discontinuity!
- Where you have treatment on one side and no (or little) treatment on the other

## Sharp Discontinuity



We usually don't graph sharp discontinuities because they are boring!

## We Can Analogize RD to an Experiment – Why?

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Because

- close to the discontinuity
- treated and untreated units
- should be observationally equivalent
- pre-treatment

What kind of estimating equation do we use for a RD?

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or

$$Y_i = \alpha_0 + \alpha_1 D + \alpha_2 (X - c) + \alpha_3 (X - c)^2 + \alpha_4 D * (X - c) + \alpha_5 D * (X - c)^2 + \alpha_6 Q + \epsilon \quad (2)$$

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Or, make  $\underline{X}$  bigger and  $\bar{X}$  smaller so that the window around  $c$  is narrower.

# Specification Matters Because Data Can Be Odd

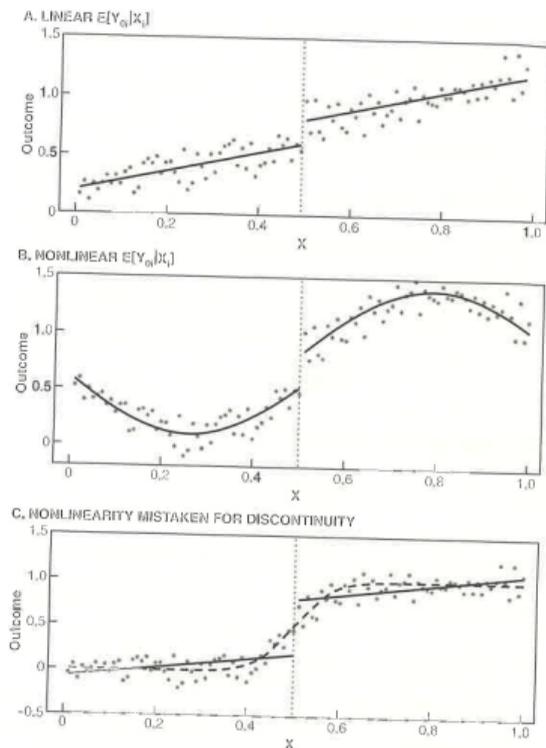


Figure 6.1.1 The sharp regression discontinuity design.

What are the testable implications for the validity of a RD design?

## What are the testable implications for the validity of a RD design?

- Discontinuity of treatment
- Continuity of pre-determined observables
- No bunching of observations at discontinuity

# RD: When it's Fuzzy

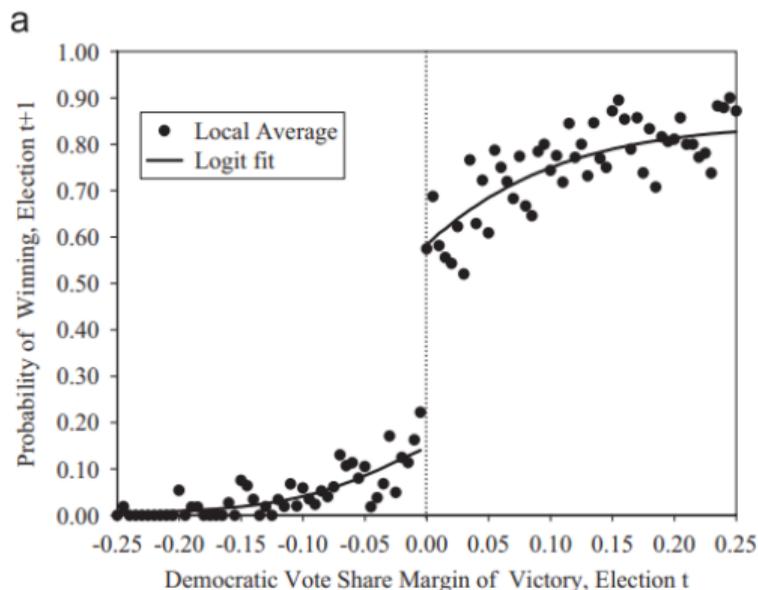
## Sharp vs Fuzzy

- Sharp RD: perfect compliance with treatment at the cut-off
- Fuzzy RD: a higher likelihood of compliance with treatment at the cut-off

## Sharp Discontinuity **Outcome** Examples

RQ: Impact of Incumbency on election at time  $t + 1$

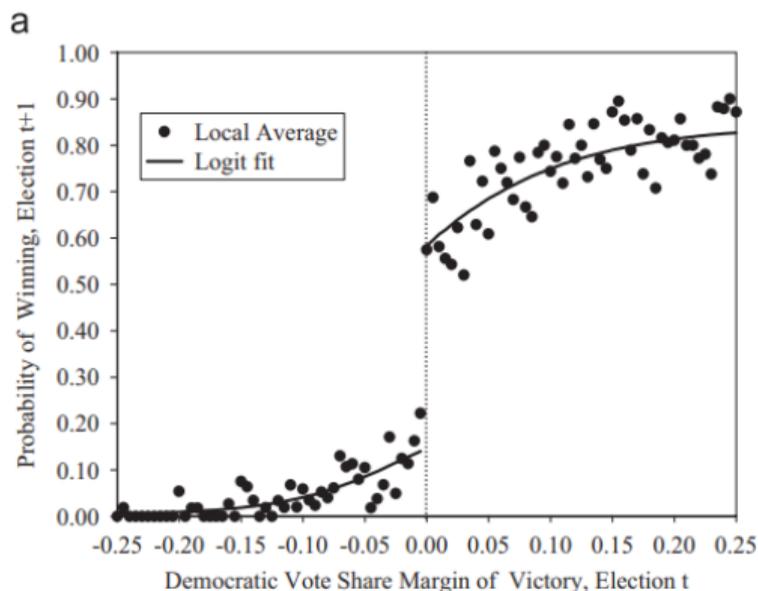
Treatment: Winning election at time  $t$



## Sharp Discontinuity **Outcome** Examples

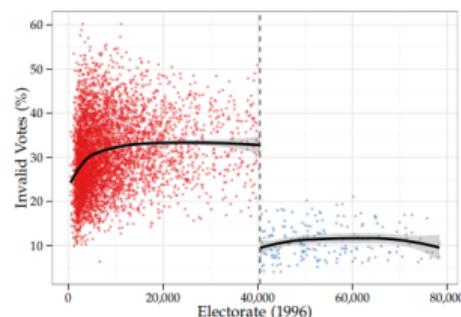
RQ: Impact of Incumbency on election at time  $t + 1$

Treatment: Winning election at time  $t$



RQ: What is the impact of electronic voting on invalid votes?

Treatment: Electronic voting, electorate  $> 40,000$



In Brazil, no paper ballots with electorate  $> 40,000$

## Fuzzy Discontinuous Treatment at Cut-off of Assignment Variable



## *MHE* Says That Fuzzy RD is IV

Recall two IV conditions

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So we can then think about fuzzy RD as a LATE, where the effect we estimate is for compliers.

# RD: Regression Kink

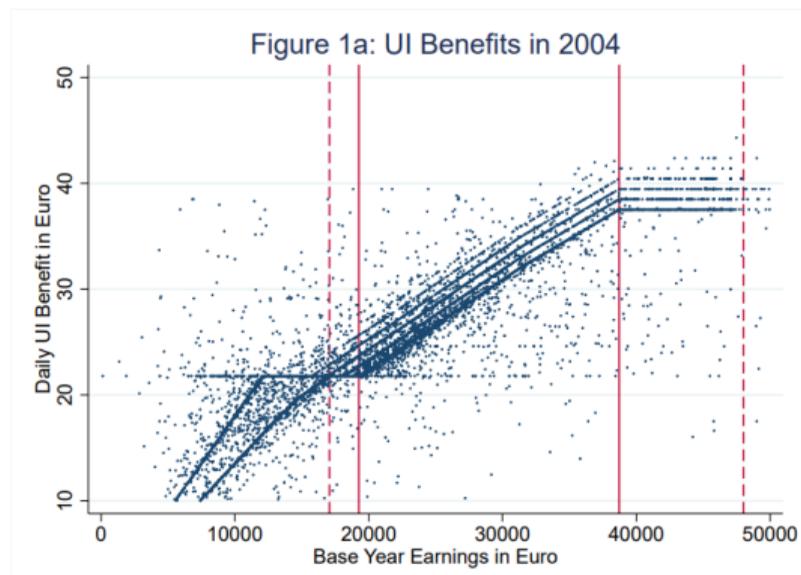
## Basic Intuition

- RD uses a break in likelihood of treatment at cut-off
- RK uses a shift in likelihood of treatment at cut-off
  - can be sharp or fuzzy

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- RD uses a break in likelihood of treatment at cut-off
- RK uses a shift in likelihood of treatment at cut-off
  - can be sharp or fuzzy
- As before, we are interested in change in  $Y$  given change in  $X$ , where the variation in  $X$  comes from the variation at the kink
- RK identification requirements from Card et al (Econometrica, 2015; pictures are from working paper version)
  - ① “conditional on the unobservable determinants of the outcome variable, the density of the assignment variable is smooth (i.e., continuously differentiable) at the kink point in the policy rule” and
  - ② “the treatment assignment rule is continuous at the kink point”
- Second one affects interpretation; not strictly necessary

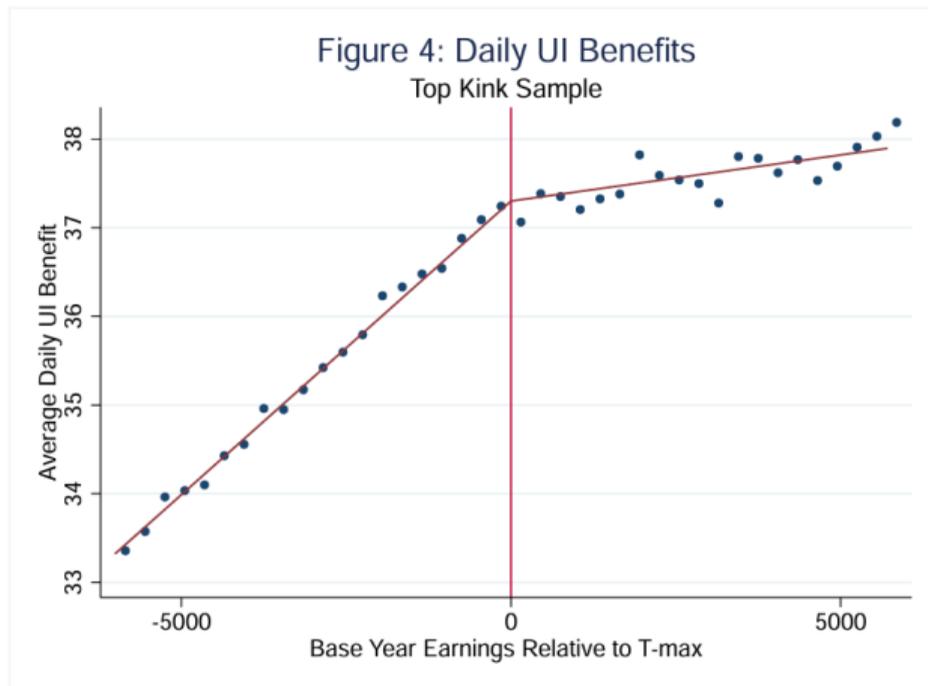
## A Treatment Example



Source: Card et al (2015) in *Econometrica*; but all figures are from NBER working paper no. 18564.

- Figure 1 is unemployment insurance receipt by income in Austria
- Lines are not drawn – those are perfect compliers with the schedule
- Authors suggest there are various errors that lead them not to get everyone on the line
- Five lines in the middle portion of the figure are for number of dependents
- We'll focus on top kink

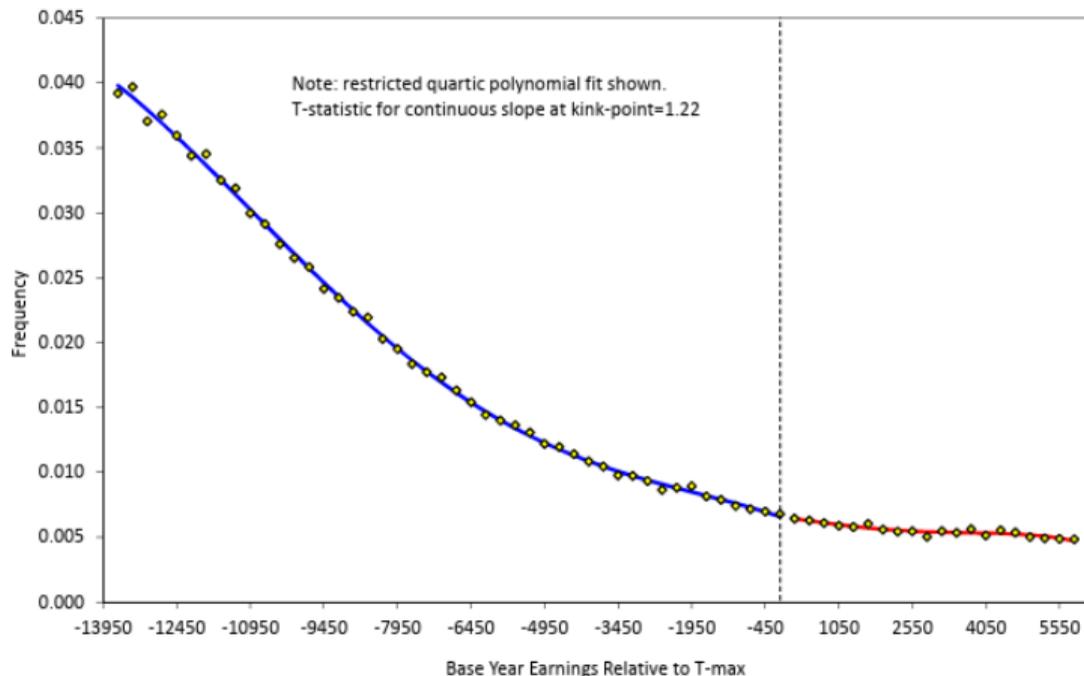
## Figure 4 Zooms in on Parts of Figure 1(a) for Single Workers



Now formulated as  $(X - c)$

## Can You Precisely Manipulate the Running Variable?

Figure 2b: Density in Top Kink Sample



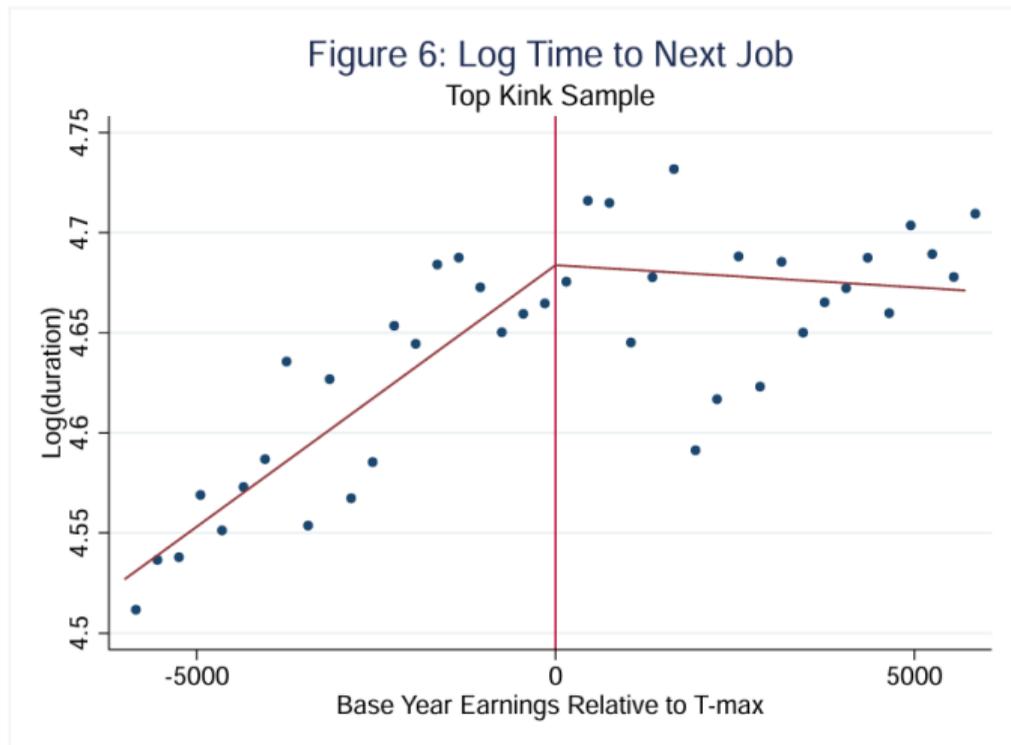
- Vertical axis is concentration of observations
- No bunching in the distribution of earnings at the kink points
- → cannot manipulate distance to the running variable

## Outcomes: How Long Does it Take to Find a New Job?



- Figure 6 is the outcome
- How long does it take you to find a new job?

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- Figure 6 is the outcome
- How long does it take you to find a new job?
- As benefits plateau, people finding jobs more quickly

## Formal statement of RK (from Card, Lee, Pei and Weber, 2012)

- Suppose we have a model  $Y = \tau b(V) + g(V) + \epsilon$ , where the kink is at  $V = v_0$
- $b(V)$  is the assignment function: how much UI you get
- $g(V)$  is how the assignment variable otherwise impacts the outcome  $Y$
- Assume
  - ① “ $b(V)$  [is] a deterministic and continuous function of  $V$ , with a kink and  $V = 0$ ”
  - ② “ $g(\cdot)$  and  $E(\epsilon|V = v)$  have derivatives that are continuous in  $V$  at  $V = 0$ ”
- Then

$$\tau = \frac{\lim_{v_0 \rightarrow 0^+} \frac{dE(Y|V=v)}{dv} | V = v_0 - \lim_{v_0 \rightarrow 0^-} \frac{dE(Y|V=v)}{dv} | V = v_0}{\lim_{v_0 \rightarrow 0^+} b'(v_0) - \lim_{v_0 \rightarrow 0^-} b'(v_0)} \approx \frac{\Delta Y}{\Delta b(V)}$$

# RD: How-to, Redux

## How-to Steps

- ① Find a discontinuity that's credible
- ② Make a graph
  - treatment variable
  - outcome variable
  - number of observations
- ③ Do a RD regression
- ④ Tests for validity

# 1. Find a Credible Discontinuity

- Ask: “are individuals able to influence the assignment variables, and if so, what is the nature of this control?”
- If
  - ① you can control the assignment variable  
AND
  - ② there is a perceived benefit (or cost) to the treatment
- → halt!

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- → halt!
- → people on one side are systematically different than people on the other

## 2. Make a Graph

Plot running variable versus

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What does this do for you?

- ① shows the RD
- ② shows the causal effect
- ③ tests for validity

## Graph Details

- Divide the assignment variable into bins
- Make sure no bins are divided by cut-off
- Calculate average treatment, outcome and number of obs for each bin
- Graph
- Graph helps you think about the right functional form for the regression
- Lets you see other jumps – which would be concerning

## What Size Bins?

- If bins are too narrow, estimates are unprecise – too noisy
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- If bins are too narrow, estimates are unprecise – too noisy
- If bins are too wide, estimates may be biased – smoothing too much by the cut-off
- Intuitively, bins should be narrow enough that there is no slope in the outcome variable within the bin (that's what causes bias)
- But there are other goals too, so this isn't the only priority
- There are “methods” but not clear answer

### 3. Do a RD regression

- In general, the form is

$$Y_i = \alpha_0 + \alpha_1 D + \alpha_2 f(X - c) + \alpha_3 D * f(X - c) + \alpha_4 Q + \epsilon$$

- What is the coefficient of interest here?

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- What is the coefficient of interest here?  $\alpha_1$
- Why do we include the  $\alpha_3$  term?

## Two RD Flavors

### Non-parametric

- kernel regressions, but these perform poorly at the boundary
- some rules about kernels may be available

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### Parametric

- assume linearity, which can also lead to bias if it's wrong
- regressions with polynomial functions of  $X$  included
  - $X + X^2 + X^3 + X^4 + \dots$
  - uses info far from the cut-off to inform us about behavior at the cut-off

## 4. Tests for Validity

- Inspect the histogram for the assignment variable
- Inspect baseline covariates versus running variable
- If things are ok, what should your graph(s) look like?

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- Inspect the histogram for the assignment variable
- Inspect baseline covariates versus running variable
- If things are ok, what should your graph(s) look like?
- No discontinuity at the discontinuity

RD: RD versus Difference in Difference

## RD versus Diff-in-diff

RD

DD

---

Fundamental Comparison

Before and after treatment cut-off

(treated before versus after) vs (untreated  
before versus after)

## RD versus Diff-in-diff

RD

DD

---

Fundamental Comparison

Before and after treatment cut-off

(treated before versus after) vs (untreated before versus after)

Estimating Equation

$$Y = \beta_0 + \beta_1 T + \beta_2 R + \beta_3 D * R + \epsilon$$

$D \equiv$  treated,  $R \equiv$  running variable

$$Y = \beta_0 + \beta_1 D + \beta_2 A + \beta_3 D * A + \epsilon$$

$A \equiv$  after

## RD versus Diff-in-diff

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Coefficient of Interest

$\beta_1$

$\beta_3$

# Manoli and Turner: Income and College Attendance

# Manoli and Turner on Income and College Attendance

- ① Research question, endogeneity and data
- ② Discontinuity, estimating equations, validity
- ③ Results

# Research Question and Endogeneity

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$$\text{attendance}_i = \beta_0 + \beta_1 \text{income}_i + \beta_2 X_i + \epsilon_i$$

- Why is this a bad idea?

# Research Question and Endogeneity

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$$\text{attendance}_i = \beta_0 + \beta_1 \text{income}_i + \beta_2 X_i + \epsilon_i$$

- Why is this a bad idea?
- Family income correlated with lots of other things that affect college going: parental education, education habits, etc.

## Manoli and Turner: Data

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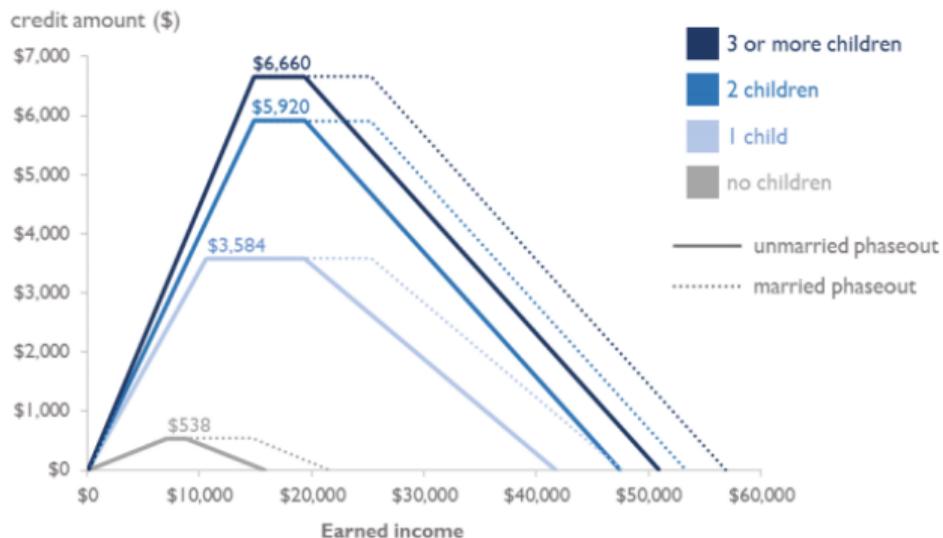
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## Manoli and Turner: Data

- What is the unit of observation?
  - Person in a year
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  - Tax data, but it seems like people are defined from social security records
- There are  $\sim 4$  million high school seniors/year in the US, so this is a selected sample
- See Appendix Table 4 for sample selection

## Manoli and Turner: EITC

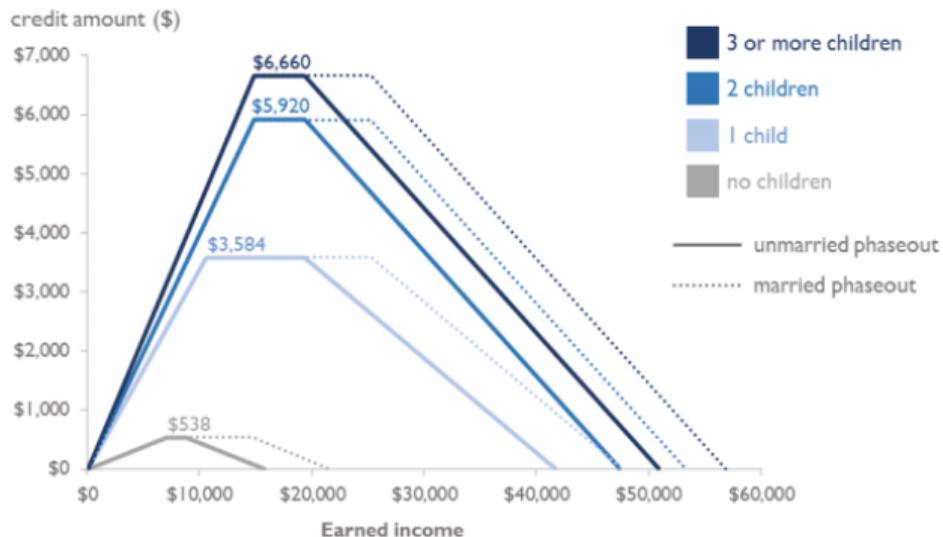
EITC Amount by Number of Qualifying Children, Marital Status, and Income, 2020



- What's the idea behind this program?

## Manoli and Turner: EITC

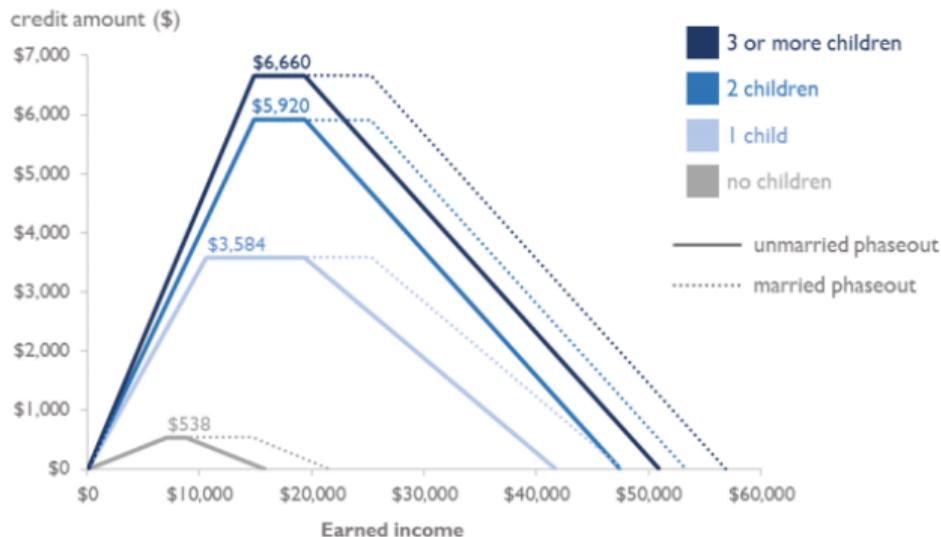
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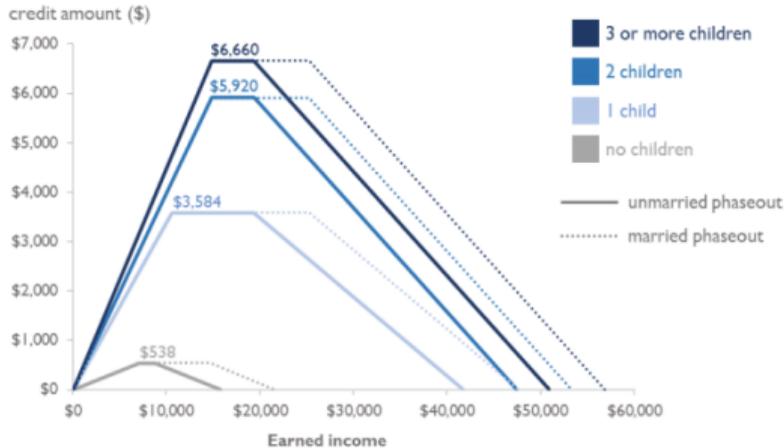


- What's the idea behind this program?
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- What does the pyramid shape of the benefit mean?
- Where might you want to lie about your income if you could? why?

# Potential Kinks

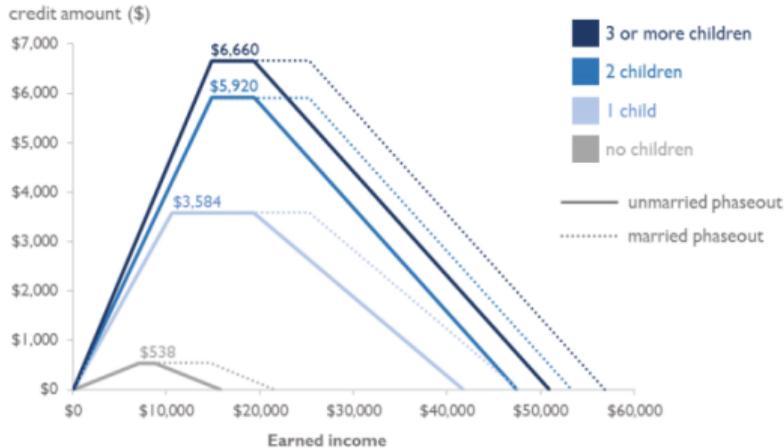
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# Potential Kinks

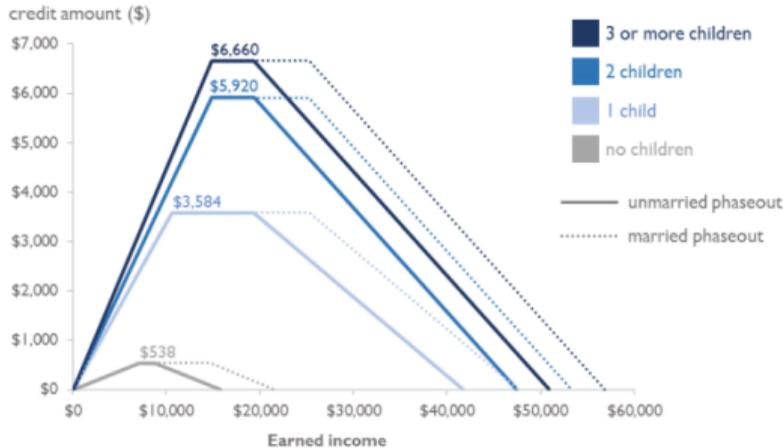
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- Why is the first kink more attractive than the second one?

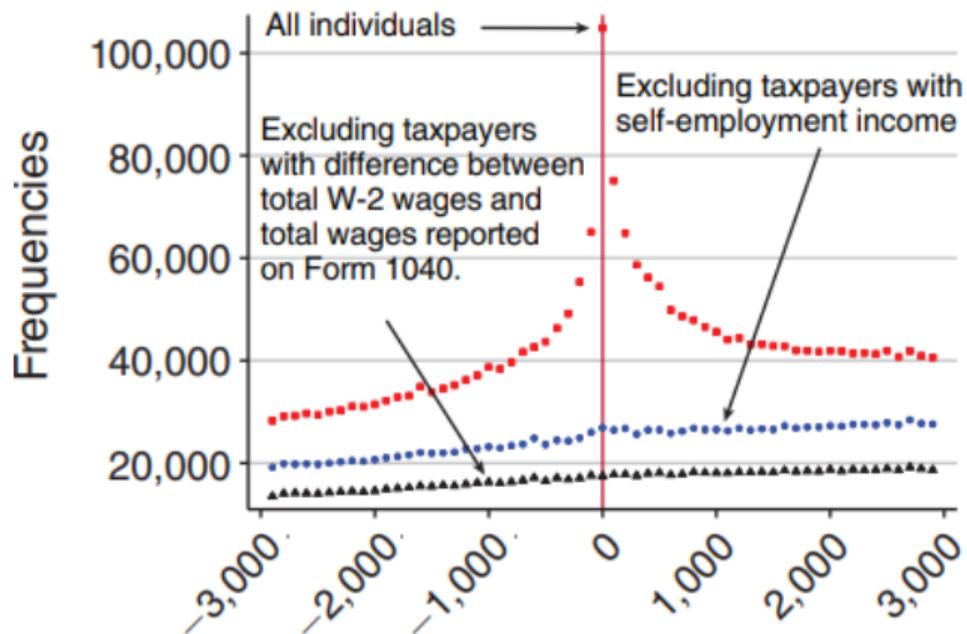
# Potential Kinks

EITC Amount by Number of Qualifying Children, Marital Status, and Income, 2020



- Where are the potential kinks in this setup?
- Why is the first kink more attractive than the second one?
  - fn 16, p. 9 says “ We have explored using a regression kink design at the second and third EITC kink points using a restricted sample that has earned income equal to AGI. ... Furthermore, when restricting to this unusual sample, we find small but statistically significant evidence of sorting along the running variable (i.e. bunching at the kink point ....)”
- What does “bunching” mean here?

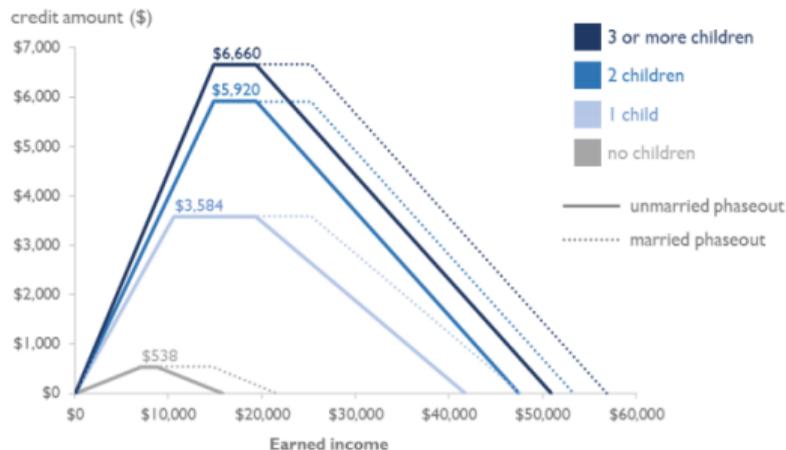
## A Bad Kink for Some People



## The Slope Comparison

On which kink in this picture are we focusing?

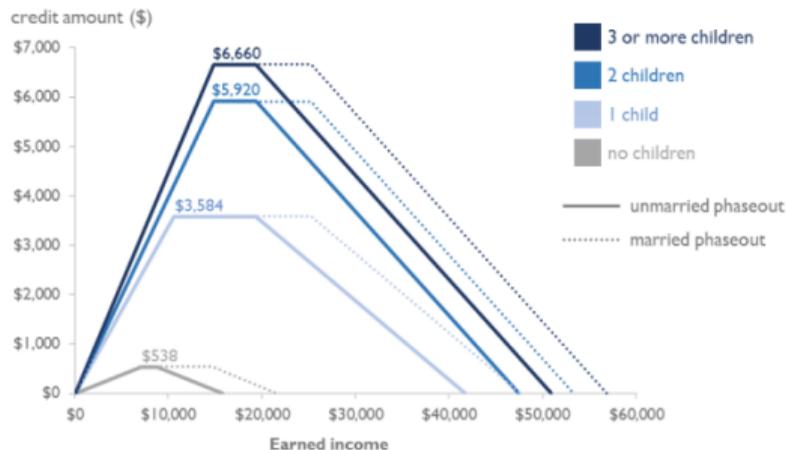
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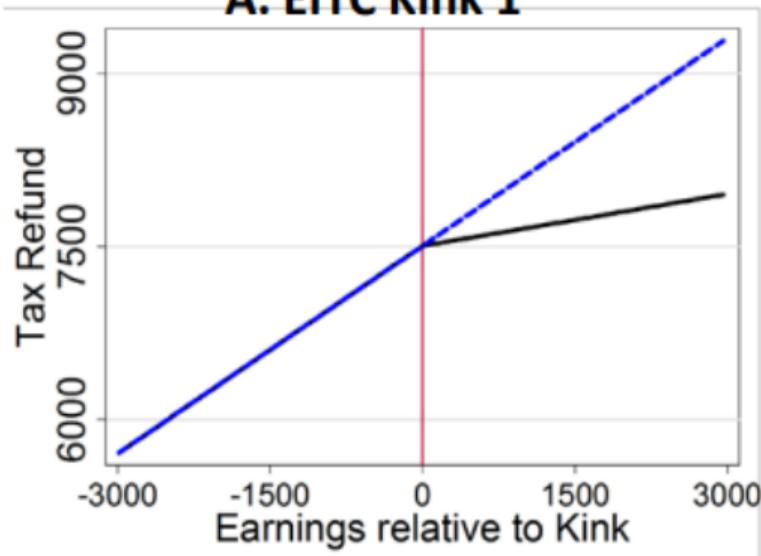
On which kink in this picture are we focusing?

EITC Amount by Number of Qualifying Children, Marital Status, and Income, 2020



Zooming in on the first kink

## A. EITC Kink 1



## Estimation

$$\text{enroll}_i = \beta \text{refund}_i + g(\text{kinkdist}_i) + \epsilon_i$$

- $\text{enroll}_i$  is 0 or 1, depending on whether you enroll in higher education in the fall following the spring refund
- $\text{refund}_i$  is the tax refund (not just EITC)
- $\text{kinkdist}_i$  is income distance to the kink
- The idea is to find the  $\hat{\beta} = \frac{\Delta \text{enrollment}}{\Delta \text{refund}}$

## Estimation, Again

But more exactly, they estimate

$$\begin{aligned}\text{enroll}_i &= \alpha \text{kinkdist}_i + \delta_e D_i \text{kinkdist}_i + \alpha_2 X_i + \epsilon_i \\ \text{refund}_i &= \gamma \text{kinkdist}_i + \delta_r D_i \text{kinkdist}_i + \alpha_2 X_i + \epsilon_i\end{aligned}$$

- $D_i = 1$  after the kink
- Note that

$$\hat{\beta} = \frac{\hat{\delta}_e}{\hat{\delta}_r}$$

- Alternatively, we could instrument for  $\text{refund}_i$  in the below with  $D_i \text{kinkdist}_i$ :

$$\text{enroll}_i = \beta \text{refund}_i + \text{kinkdist}_i + \epsilon$$

## Estimation Intuition

$$\beta = \frac{\text{enrollment rate of change, post cut-off} - \text{enrollment rate of change, pre cut-off}}{\text{refund rate of change, post cut-off} - \text{refund rate of change, pre cut-off}}$$

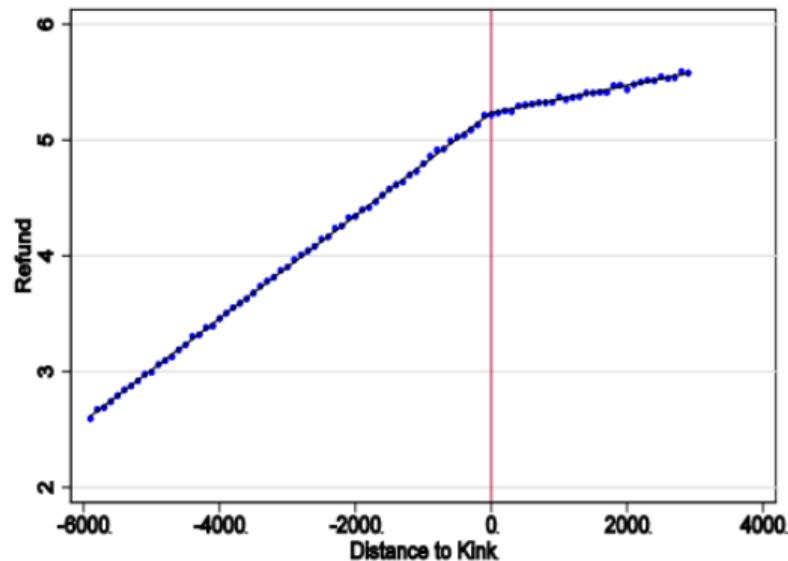
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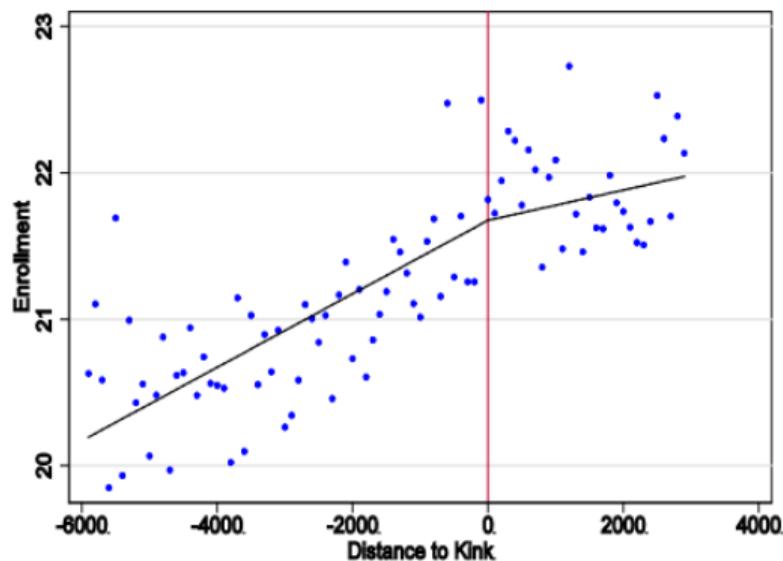
In a sharp RD, analogous denominator is 1!

## Results In Pictures

### A. Change in Tax Refund



### B. Change in Enrollment



## Results in Table

- How do we interpret the top two coefficients?

Table 2: RKD Estimates

	Full Sample		1 Child	
	First Stage Refund	Reduced Form Enrollment	First Stage Refund	Reduced Form Enrollment
Slope Change	-0.343 (0.002)	-0.147 (0.060)	-0.337 (0.001)	-0.152 (0.107)
Effect of \$1000 on Enrollment (IV)		0.430 (0.175)		0.450 (0.317)
N		1,427,447		465,745

Notes: Each coefficient is estimated from a separate regression. Each regression includes dummy variables for filing status. Standard errors are clustered based on \$100 bins of earnings relative to the kink point.

## Results in Table

- How do we interpret the top two coefficients?
  - An extra \$1,000 dollars yields a -0.343 change in the slope of the refund

Table 2: RKD Estimates

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- Remember this is a change in the rate of change
- IV result is 0.430 (about -0.147/-0.343)
- Interpretation? An additional \$1k of refund yields 0.43 pp increase in enrollment

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## Validity Tests

- What are the two key underlying assumptions?

## Validity Tests

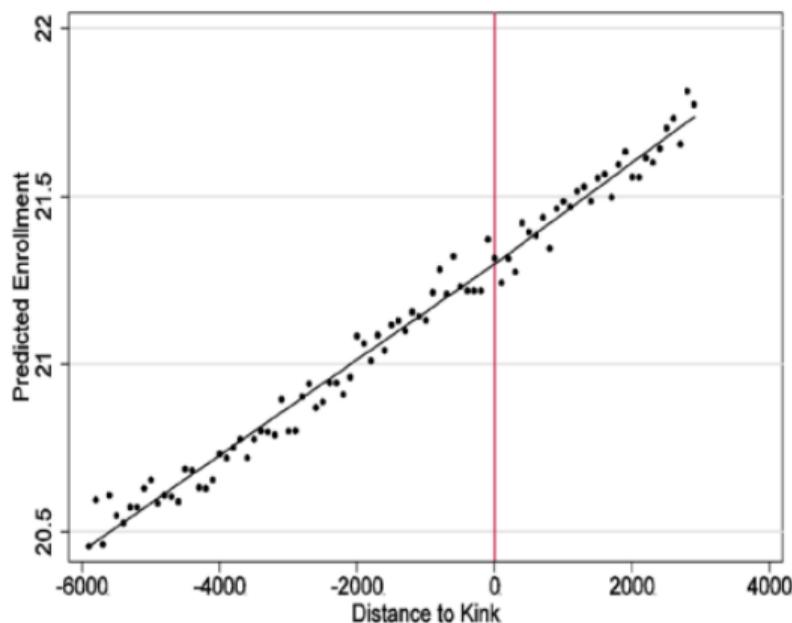
- What are the two key underlying assumptions? (listed p. 14)
  - ① “other covariates do not change at the kink points” and
  - ② “taxpayers do not sort along the tax schedule”
- And, implicitly, that their kink is important
- What kind of evidence can you show on this?

# 1. “Other Covariates Do Not Change at the Kink Points”

- Put all covariates together into “predicted enrollment”
- What is this “predicted enrollment”?

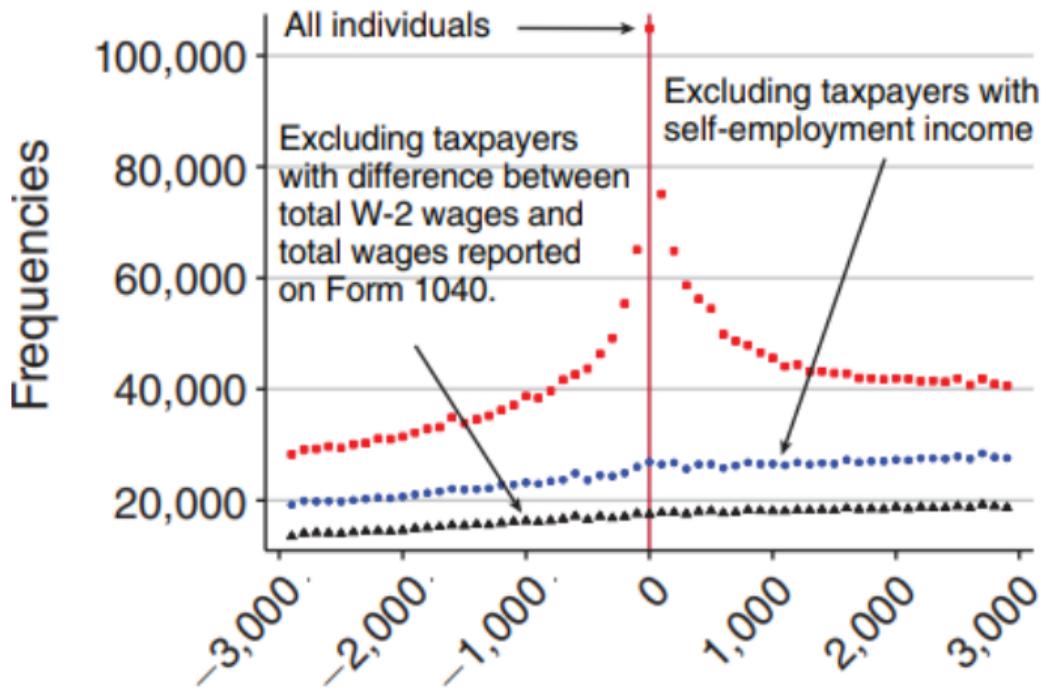
$$\text{enrollment}_i = \gamma X_i + \epsilon_i$$

- Make  $\widehat{\text{enrollment}}_i = \hat{\gamma} X_i$
- A way to combining a bunch of covariates into one
- Footnote 19 says individual covariates could have a kink even if their aggregate does not. They say it's not true, but don't say more than that.



## 2. “Taxpayers Do Not Sort Along the Tax Schedule”

- How do we do this?
- Look at number of people around the kink



## More Implicit: This is an Important Kink

- How can we tell if this kink is important?

## More Implicit: This is an Important Kink

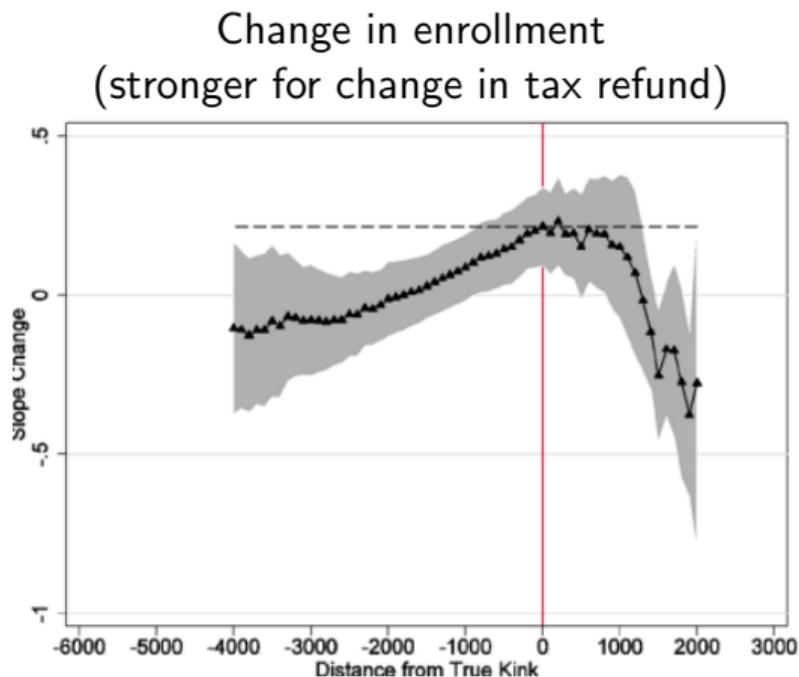
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- How can we tell if this kink is important?
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  - at the true kink
  - the move the kink location around and look for differences

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## RD and RK: Big Picture

- RD is a near-experimental method for identifying causal effect
- Requires sharp change at cut-off
- Credible only when you also show
  - no bunching at cut-off
  - continuity of covariates at cut-off

## Next Lectures

- Next two classes on matching
- Matching 1
  - comment on my paper, and it's ok to complain
- Next class: quantitative summary due