Opp. Costs

AC and MC

Lecture 9: Costs

October 24, 2023



Course Administration

- 1. Problem Set 8 posted
- 2. Use Numbers 3 posted





Course Administration

- 1. Problem Set 8 posted
- 2. Use Numbers 3 posted
- 3. Midterm return and curve next slide
- 4. Any questions?



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Cost Curves

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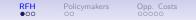
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Midterm Results

Score >	Score \leq	Grade	Number
50	59	B-	4
60	69	В	3
70	79	B+	1
80	89	A-	3
90	99	А	3

- If you are on the border of a letter grade, I round up
- If you got an A and are willing to volunteer to help a student, email me
- If you got a B- or below and would like a student partner, please let me know
- Nov. 6, 10:30 to 11:30 am: midterm review – come to ask questions

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Next Week: Ripped from the Headlines

Send article by Wednesday midnight.

Finder	Presenter
Emily	Vanea

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This Week: Ripped from the Headlines

Finder	Presenter
Trenton	Kari

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- Basics and assumptions
- Short run
- Long run
- Cost minimization
- Economies of scale, returns to scale, returns to scope
- Total cost

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Costs and Policymakers



• Supply costs determine economies of scale





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- Supply costs determine economies of scale
 - big investment in mRNA covid vaccines and infrastructure
 - invest in a few big firms, or many little ones?
 - depends upon returns to scale

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Policymakers

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- but infeasibly expensive due to landowner opposition and transmission line costs

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 - see recent subsidies for computer chip industry
 - unclear if this is enough

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Policymakers

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 - see recent subsidies for computer chip industry
 - unclear if this is enough
- Government is frequently a producer itself
 - how many fighter aircraft do we need to provide defense?



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Economic Costs vs. Accounting Costs



Economic Costs vs. Accounting Costs

- Accounting cost \equiv direct cost
- Opportunity cost \equiv cost of what you give up by using an input
 - · Perhaps most easily thought of as next best opportunity for funds
 - What's the opportunity cost of pursuing a MPP?



Economic Costs vs. Accounting Costs

- Accounting $cost \equiv direct cost$
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 - Give an opportunity cost example



Economic Costs vs. Accounting Costs

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 - What's the opportunity cost of pursuing a MPP?
 - Give an opportunity cost example

Economic cost \equiv accounting cost + opportunity cost

Opportunity Cost in Policy Action: VW Fraud

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• 2008 to 2015, VW markets "Clean Diesel" low emissions technology

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- But vehicles have "defeat device" that gives low emissions for tests only
- Federal Trade Commission has to figure out how much VW should pay consumers
- Usually rely on "replacement cost" but that doesn't work here because there is no replacement for this non-existing product



Use Opportunity Cost to Value Damage

• Before fraud was revealed, consumers had a high level surplus from VW clean diesel

• Fraud destroys surplus!



Use Opportunity Cost to Value Damage

• Before fraud was revealed, consumers had a high level surplus from VW clean diesel

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- Fraud destroys surplus!
- Value damage by comparing
 - Consumer surplus after learning about VW fraud to
 - Consumer surplus from next best alternative



- Before fraud was revealed, consumers had a high level surplus from VW clean diesel
- Fraud destroys surplus!
- Value damage by comparing
 - Consumer surplus after learning about VW fraud to
 - Consumer surplus from next best alternative
- FTC's components of consumer injury
 - 1. Lost opportunity to avoid excess pollution

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- 2. Price premium for clean emissions via comparison to other vehicle
- 3. For those who choose emissions repair, compensation for performance reduction

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4. Additional transaction costs from this remedy

Thanks to Mary Sullivan for this example, and find FTC report here.



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Opportunity Costs in Government

The Atlantic

Buses Shouldn't Be Free

The push for fareless transit is downstream of a larger failure: American urban elected officials have struggled to improve government services, especially infrastructure development.

By Jerusalem Demsas

Neurolettere



- Late 2022 DC council considered making WMATA buses free in the city
- Argues that transit riders care more about service than cost
- Cutting fares has an opportunity cost what is it?

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- Late 2022 DC council considered making WMATA buses free in the city
- Argues that transit riders care more about service than cost
- Cutting fares has an opportunity cost what is it?
- "Focusing on zero-dollar rides is like overseeing a library system stocked solely with out-of-date self-help books in crumbling buildings and wondering if a fresh coat of paint will improve morale."

"Buses Shouldn't Be Free," The Atlantic, December 9, 2022. [link]

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Sunk Costs

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- Firm has some fixed costs
- If the firm went bankrupt, some of those costs could be recovered
- The non-recoverable part of the fixed costs is called "sunk" or sunk costs

• Examples?



- When costs are sunk, they should not enter into future business decisions
- Making decisions based on sunk costs is known as the "sunk cost fallacy"

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• Decisions should be forward-looking: sunk costs are gone

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				Costs Ex. Profit					
	Mo.	Ex. Rev.	Total	Sunk	Addt'l	Continue	No Prod.		
	June	150	-100	-16	-84	50	-16	-	



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• June: Ex. Profit > 0, clearly should go ahead.



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Dec.	150	-175	-140	-25	-25	-140	



- June: Ex. Profit > 0, clearly should go ahead.
- Sept.: Ex. Profit still > 0.
- Dec.: Ex. Profit < 0. Halt production? No, because alternative is loss of 140.^a

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Fixed & Variable Costs Cost Curves



- Fixed costs \equiv costs that do not depend on how much output the firm produces
- Variable costs \equiv costs that do vary with the firm's output



What Determines Whether the Cost is Fixed or Variable?

Time Horizon

- Many things are fixed in the short run
- Nothing is fixed in the long run



What Determines Whether the Cost is Fixed or Variable?

Time Horizon

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Other Factors

- Active rental markets can turn fixed costs into variable costs
- Long-run labor contracts can make labor a fixed, rather than variable cost

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- Total cost recall the expansion path!
- Fixed cost
- Variable cost

TC = FC + VC.

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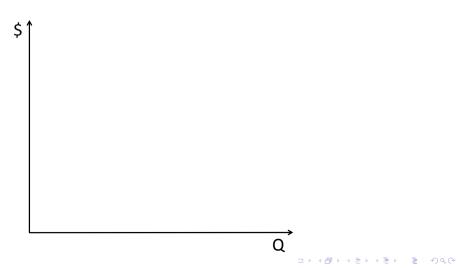
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Drawing TC, FC and VC

What Does the Total Cost Curve Look Like?



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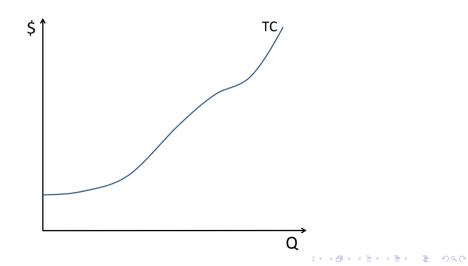
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Drawing TC, FC and VC

What About the Variable Cost Curve?



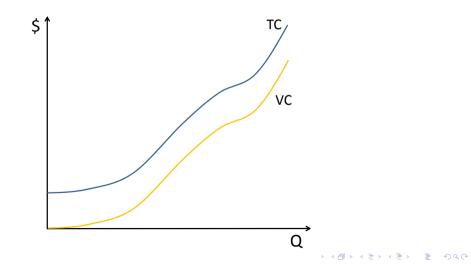
Drawing TC, FC and VC

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And the Fixed Cost Curve?



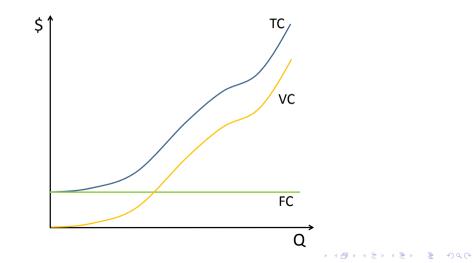
Drawing TC, FC and VC

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Everyone, Together



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Average & Marginal Costs

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Definitions

- Average total costs: $ATC = \frac{TC}{Q}$
- Average fixed costs: $AFC = \frac{FC}{Q}$
- Average variable costs: $AVC = \frac{VC}{Q}$



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Definitions

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What about the shapes?

• AFC



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What about the shapes?

- AFC
- AVC remember the law of diminishing returns



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What about the shapes?

- AFC
- AVC remember the law of diminishing returns
- *ATC*

Note that because there are fixed costs, this must be the short run.



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Average Costs in Pictures

What Does Average Fixed Cost Look Like?





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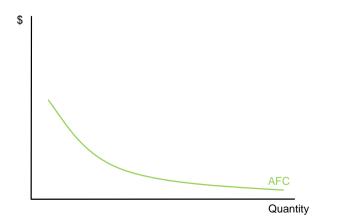
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Average Costs in Pictures

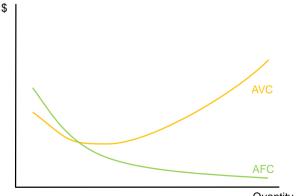
What About Average Variable Costs?



Average Costs in Pictures

Opp. Costs

And Average Total Cost?

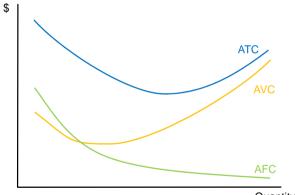


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Everyone, Together



Quantity



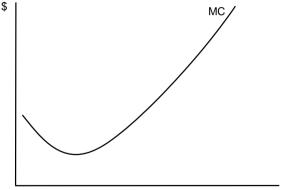
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- Marginal cost \equiv additional cost to produce an additional unit of output
- Without calculus, $MC = \frac{\Delta C}{\Delta Q}$, or the slope of the total cost curve
- With calculus, $MC = \frac{\partial C}{\partial Q}$
- What is its shape?



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Average vs. Marginal Cost

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$$ATC = \frac{TC}{Q}$$
$$MC = \frac{\Delta C}{\Delta Q} = \left(\frac{\partial C}{\partial Q}\right)$$

Both come from total cost

,

• When MC < ATC, what happens to average cost as Q increases?

Average vs. Marginal Cost

$$ATC = \frac{TC}{Q}$$
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Both come from total cost

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- When MC < ATC, what happens to average cost as Q increases? decreases
- When MC > ATC, what happens to average cost as Q increases?

SR and LR

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Average vs. Marginal Cost

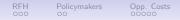
AC and MC

$$ATC = \frac{TC}{Q}$$
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Both come from total cost

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- When MC < ATC, what happens to average cost as Q increases? decreases
- When MC > ATC, what happens to average cost as Q increases? increases
- \rightarrow *MC* = *AC* \rightarrow *AC* must be at a minimum
- \rightarrow *MC* curve intersects *AC* curve at minimum



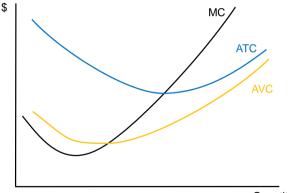
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Average and Marginal Costs



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Relationship Between Costs

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Relationship Between Costs

The filled in boxes.								
тс	FC	VC	MC					
5	5	0	0					
15	5	10	10					
23	5	18	8					
28	5	23	5					
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Short Run & Long Run Costs

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In the long run, nothing is fixed.

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Implications of No Fixed Costs in Long Run

- Long run costs are never higher than short run costs
- Long run average cost curve intersected by marginal cost curve at the same place as the short-run average cost curve (where's that?)



Implications of No Fixed Costs in Long Run

- Long run costs are never higher than short run costs
- Long run average cost curve intersected by marginal cost curve at the same place as the short-run average cost curve (where's that?)

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- the minimum of the average cost curve
- But all costs in the long run are variable

An In-Class Problem: Costs

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Suppose a firm's total cost curve is $TC = 10Q^2 + 6Q + 60$, and the marginal cost curve is MC = 20Q + 6.

- 1. Find an expressions for the firm's
 - 1.1 fixed cost
 - 1.2 variable cost
 - 1.3 average total cost
 - 1.4 average variable cost
- 2. Find the output level that minimizes average total cost.
- 3. Find the output level that minimizes average variable cost.
- 4. If MC = 20Q + 6 were the firm's long run marginal cost, could $MC_{SR} = 15Q + 6$ be the firm's short-run marginal cost?

In-Class Problem Answer

1. Expressions for

1.1 Fixed cost: The part of output not a function of price – or costs when output is zero \rightarrow FC = 60

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- 1.2 Variable cost: Recall that $TC = FC + VC \rightarrow 10Q^2 + 6Q + 60 = 60 + VC$, or $VC = 10Q^2 + 6Q$
- 1.3 Average total cost: ATC = C/Q = 10Q + 6 + 60/Q
- 1.4 Average variable cost: $AVC = VC/Q = 10Q^2 + 6Q = 10Q + 6$.
- 2. Output level that minimizes average total cost: Recall that ATC is at a minimum where $ATC = MC \rightarrow 10Q + 6 + 60/Q = 20Q + 6$, or $10Q + 60/Q = 20Q \rightarrow 10Q = 60/Q \rightarrow 10Q^2 = 60 \rightarrow Q^2 = 6 \rightarrow Q = \sqrt{6}$
- 3. Output level that minimizes AVC is where $AVC = MC \rightarrow 10Q + 6 = 20Q + 6 \rightarrow 10Q = 0 \rightarrow Q = 0$. Remember that AVC increases with production.
- 4. We know that $MC_{SR} \ge MC_{LR}$, $15Q + 6 \le 20Q + 6$, so, no.

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Scale: Returns, Economies, and Scope

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Three Separate but Related Concepts

- 1. Returns to scale
- 2. Economies of scale
- 3. Economies of scope



Returns to Scale \equiv changes in output given a change in inputs, where the inputs increase in fixed proportions.



Returns to Scale \equiv changes in output given a change in inputs, where the inputs increase in fixed proportions.

What does "fixed proportions" mean?

- Suppose your firm uses 20 units of capital and 30 units of labor
- This is a capital-labor ratio of $\frac{20}{30}$
- Any combination of K and L that gives a ratio of $\frac{2}{3}$ is in **fixed proportions**

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• Give me some examples!



Flavors of Returns to Scale

- 1. Constant \rightarrow outputs increase proportionately with inputs
- 2. Increasing \rightarrow outputs increase more than proportionately with inputs
- 3. Decreasing \rightarrow outputs increase less than proportionately with inputs

• Suppose your production function is

Opp. Costs

Q = 5K + L

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Economies

• Suppose your production function is

Q = 5K + L

Economies

• Double inputs: K' = 2K, L' = 2L – note this is keeping inputs in fixed proportions

• Suppose your production function is

Q = 5K + L

AC and MC

Economies

- Double inputs: K' = 2K, L' = 2L note this is keeping inputs in fixed proportions
- Find new Q, call it Q', relative to old Q

Suppose your production function is

$$Q = 5K + L$$

AC and MC

Economies

- Double inputs: K' = 2K, L' = 2L note this is keeping inputs in fixed proportions
- Find new Q, call it Q', relative to old Q

$$egin{aligned} Q' &= 5 {\cal K}' + L' \ &= 5(2 {\cal K}) + (2 L) \ &= 2(5 {\cal K} + L) \ &= 2 Q \end{aligned}$$

Suppose your production function is

$$Q = 5K + L$$

AC and MC

Economies

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• Double inputs: K' = 2K, L' = 2L – note this is keeping inputs in fixed proportions

• Find new Q, call it Q', relative to old Q

$$Q' = 5K' + L'$$

= 5(2K) + (2L)
= 2(5K + L)
= 2Q

We call this constant returns to scale.



Flavors of Returns to Scale

1. Constant \rightarrow outputs increase proportionately with inputs

• double inputs, double outputs



Flavors of Returns to Scale

- $1. \ \mbox{Constant} \rightarrow \mbox{outputs}$ increase proportionately with inputs
 - double inputs, double outputs
- 2. Increasing \rightarrow outputs increase more than proportionately with inputs
 - double inputs, more than double outputs



Flavors of Returns to Scale

- 1. Constant \rightarrow outputs increase proportionately with inputs
 - double inputs, double outputs
- 2. Increasing \rightarrow outputs increase more than proportionately with inputs
 - double inputs, more than double outputs
- 3. Decreasing \rightarrow outputs increase less than proportionately with inputs
 - double inputs, less than double outputs

Admin RFH Policymakers Opp. Costs Sunk Costs Cost Curves AC and MC SR and LR Economies 00 00 0000 0000 0000 00000 00000 00000 00000

Flavors of Returns to Scale

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 - double inputs, double outputs
- 2. Increasing \rightarrow outputs increase more than proportionately with inputs
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In general, put in inputs, find Q.

Double the inputs, find Q'. Is Q' = 2Q? Q' > 2Q? Q' < 2Q?



What Drives Returns to Scale?

- Increasing returns
 - Fixed costs
 - Learning by doing if the firm gets bigger and better at production by producing

- Decreasing returns
 - Regulation
 - Limited low cost/high quality inputs (violates one of our assumptions)

Admin RFH Policymakers Opp. Costs Sunk Costs Cost Curves AC and MC SR and LR Economies 00 000 0000 0000 00000 000000 00000 000000 00000 00

Now, Economies of Scale

Economies of scale \equiv a firm's the ability to produce at a lower per-unit cost at higher levels of production.

Now, **Economies** of Scale

AC and MC

Economies

Economies of scale \equiv a firm's the ability to produce at a lower per-unit cost at higher levels of production.

- Economies of scale \equiv
 - output increases more rapidly than total cost
 - double total cost, more than double output
- Diseconomies of scale \equiv
 - output increases more slowly than total cost
 - double total cost, less than double output
- Constant economies of scale \equiv
 - total cost and output increase as same rate
 - double total cost, double output

Now, **Economies** of Scale

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You can see these in the shape of the average cost curve.

Economies



Economies of Scale vs. Returns to Scale

Returns to scale

• Does increase in inputs increase output? By how much?



Economies of Scale vs. Returns to Scale

Returns to scale

- Does increase in inputs increase output? By how much?
- Economies of Scale
 - Does increase in costs increase output? By how much?



Economies of Scale vs. Returns to Scale

Returns to scale

- Does increase in inputs increase output? By how much?
- Economies of Scale
 - Does increase in costs increase output? By how much?

Therefore

- Increasing returns to scale \implies economies of scale
- Economies of scale \implies returns to scale



Economies of Scale vs Returns to Scale

Returns to Scale

- You use 5 units of K and 3 units of L
- This costs \$100
- Gives output of 20



Economies of Scale vs Returns to Scale

Returns to Scale

- You use 5 units of K and 3 units of L
- This costs \$100
- Gives output of 20
- Now you use 10 units of K and 6 units of L
- Do you make more or less than 40 units of output?



Economies of Scale vs Returns to Scale

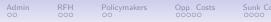
Returns to Scale

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Economies of Scale

• You use \$100 to produce output of 20

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Cost Curves

AC and MC S

SR and LR 00000

Economies of Scale vs Returns to Scale

Returns to Scale

- You use 5 units of K and 3 units of L
- This costs \$100
- Gives output of 20
- Now you use 10 units of K and 6 units of L
- Do you make more or less than 40 units of output?

Economies of Scale

• You use \$100 to produce output of 20

- Now you can spend \$200
- Do you make more or less than 40 units of output?



Economies of Scope

- Economies of scope ≡ firm produces multiple outputs more cheaply together than it would each individual output
- Diseconomies of scope \equiv firm produces multiple outputs at a higher cost than it would if it produced each output individually

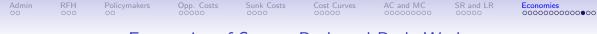
• Where do they come from?



Economies of Scope

- Economies of scope ≡ firm produces multiple outputs more cheaply together than it would each individual output
- Diseconomies of scope ≡ firm produces multiple outputs at a higher cost than it would if it produced each output individually

- Where do they come from?
- From sharing common inputs or knowledge



Economies of Scope: Bath and Body Works

• What do they produce?

Bath & Body Works[®]

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Economies of Scope: Bath and Body Works

- What do they produce?
- What could economies of scope be?

Bath & Body Works[®]



Bath & Body Works[®]

- What do they produce?
- What could economies of scope be?
- *Wall Street Journal* says that onshoring production enhances economies of scope

AC and MC

Economies

Economies of Scope: Bath and Body Works

Bath & Body Works[®]

- What do they produce?
- What could economies of scope be?
- *Wall Street Journal* says that onshoring production enhances economies of scope

AC and MC

Economies

- respond more rapid to market changes
- create lots of flavors



- Opportunity Costs
- Sunk Costs
- Cost Curves: Total Cost = Fixed Cost + Variable Cost
- Average Cost and Marginal Cost
- Short Run and Long Run Costs
- Economies of Scale (and maybe Scope)



- Read GLS Chapter 8
- Skip 8.5

